

A. Seitmuratov¹, Z.A. Yergalauova², L.S. Kainbayeva¹, G.K. Yeshmurat¹

¹Korkyt Ata Kyzylorda State University, Kyzylorda, Kazakhstan

²Abai Kazakh National Pedagogical University, Kazakhstan

E-mail: angisin@mail.ru, zina_73er@mail.ru, larissa_kain@mail.ru, gulnuresh@mail.ru

PROBLEMS AS METHOD OF THE PROFESSIONAL ORIENTATION OF TEACHING MATHEMATICS AT TECHNICAL SPECIALTIES OF HIGHER EDUCATIONAL INSTITUTION

Abstract. The article deals with the problem of the professional orientation of teaching mathematics at technical specialties of a higher educational institution and the analysis of the resources concerning the solution of problems with professional content, their selection and ranking has been made as well. The article focuses on the didactic conditions that professionally oriented problems must coincide with in training future engineers for their successful application, the classification of problems with professional content, as well as ways to solve such problems. The main requirements for problems with professional content are shown and the problem on the theme "Application of a certain integral to pressure calculation" is considered.

Keywords: problem, complexity level, professional orientation, classification of problems.

The modern development of the economy in our country needs specialists who can construct mathematical models of various processes and phenomena at various levels. The students' mastering of theoretical knowledge in the field of mathematics is not enough to implement the learning objectives. The students need to be able to use their knowledge in various situations. One of the ways to implement this approach is the multidimensional application of the interdisciplinary relations of mathematics with general scientific and major disciplines, that is, the application of applied and professionally oriented problems at mathematics classes. Most researchers studying the problems of the applied orientation of teaching mathematics at the technical specialties of the university believe that the most effective method of improving the quality of mathematical education and the process of teaching mathematics is teaching the problems with professional content.

The mathematical model of the applied problem reflects the real situation that arises in reality through mathematical symbols, signs and relations between them. In the process of constructing a mathematical model, the concrete objects of reality are replaced by their mathematical equivalents.

Vilenkin N.Ya. [1, p.29] distinguishes the following stages in modeling:

- identifying significant factors and discarding inessential ones in a situation or phenomenon;
- constructing the relationship scheme of the essential factors of the situation (phenomenon);
- obtaining the required conclusions from the constructed scheme.

Further, Vilenkin N.Ya. continues that in order to implement the described content of the modeling process, one must:

- know some objects, relationships and facts of a certain field of activity;
- be able to discard the inessential factors and distinguish the main ones in the situation under consideration;

- create a scheme of the situation (phenomenon) on a received basis;
- select the "language" in which the received scheme will be considered;
- get the required conclusions from the scheme, i.e. solve the problem in the selected "language".

Solving problems in teaching is an important stage in the formation of the cognitive activity of a student. In the process of solving problems, abstraction and formalization take place, synthesis, analysis, generalization, etc. are performed, all mental processes are aggravated.

D. Poya [2, p. 56] identifies the following steps in solving problems:

- 1) to understand the condition of the problem assigned;
- 2) to analyze the problem;
- 3) to create a mathematical model of the problem;
- 4) to carry out the synthesis, i.e. implement the solution found;
- 5) to check and assess the result.

A.M. Matyushkin [3, p.36] proposes the structure for solving problems as follows:

- 1) the "closed" solution, i.e. application of standard solution methods;
- 2) the "open" solution, i.e. finding non-standard methods;
- 3) the implementation of the found method of solution;
- 4) the check of the solution result.

In our research, we use the term "problem with professional content".

The problems with professional content must be composed as follows:

1. Formulation of the problem conditions;
2. Initial data for solving the problem;
3. Additional questions;
4. Referenced data (appendix).

Theoretical knowledge, skills and abilities acquired for a certain period of time in various disciplines are accumulated in problems with professional content. The condition for such problem should contain professional elements. Information from courses of physics, chemistry, theoretical mechanics, electrical engineering, etc. can be used in such a problem. Therefore, the problem with professional content is integral in its nature, i.e. it combines mathematical theories and knowledge of major disciplines. The integrity of the problem with professional content is one of the pedagogical functions assigned to it.

One of the didactic issues relating to problems with professional content is the *selection of problems* included in the educational and methodical complex.

B.S. Kaplan, N.K. Ruzin, A.A. Stolyar believe that "in particular, learning through problems defines the thorough selection of problems, their grouping in specific sequences that allow constructing of a solution process like a research process. At the same time, one can reveal the possibilities of generalizing problems, formulating and solving new ones, and achieving a new, sometimes unexpected theoretical result, deepening the meanings of the objects studied by solving a sequence of problems".

The selection and making up mathematical problems with professional content have a few stages.

Stage 1. The analysis of normative documentation (standards, standard plans, etc.) and the requirements for a future engineer in a given area of specialization in future professional activity. The main component here is the professional qualification of the future specialist. At the first stage, the following should be identified:

1. knowledge required to study general scientific, major, technical disciplines;
2. skills and abilities acquired in solving problems with professional content;
3. quality (moral, professional).

Let us consider the second stage in the formation of a set of problems with professional content.

Stage 2. The determination and systematization of the content of higher mathematics course aimed at achieving the goals. The determination of the goals for studying specific themes, sections required in teaching a series of general scientific and major disciplines.

Stage 3. The direct formation of a series of applied and professionally oriented problems, taking into account the identified peculiarities, the thematic division of problems and ranking them based on level of complexity. One can divide the content of problems into modules of themes studied.

Based on the analysis of the above mentioned research, we distinguish the key points that determine the quality of the formation of mathematical thinking in solving problems with professional content:

- ability to transform practical problems into a mathematical language (the ability to mathematical modeling);
- logical construction in reasoning;
- ability of spatial mathematical thinking;
- accuracy of symbols when replacing a real research object with its analogue;
- accurate analysis of the problem;
- search for the best method to solve the problem;
- prediction of a possible result;
- interpretation of the result obtained, i.e. "transformation" into the original "language".
- quality assessment of the result.

The selection of problems with professional content should be aimed at achieving the following goals:

- help the student to master the general principles of the mathematical apparatus as a means of solving the theoretical and practical problems of engineering;

- facilitate the study of a number of important disciplines that form the basis of specialist's education;

As a conclusion, we will define the requirements for problems with professional content for engineering and technical specialties:

- the problem should contain a real situation arising in the professional activities of engineers;
- the numerical data used in the problem must be real;
- the problem must include the interdisciplinary relationship;
- the problem must have practical value, the significance of mathematical knowledge should be revealed in it;
- depending on the complexity the problem must have different levels, i.e. they must be formed on the principle "from simple to complex".

The ranking of problems is carried out by the lecturer, and students can choose the level corresponding to them at the moment. The first level is aimed at developing skills and abilities in the process of solving problems, the solution algorithm of which is known (algorithmic, training). The second level of the problem complexity is the formation of skills and abilities of solving problems when the algorithm is not completely known (reduction to known algorithms or a superposition of a number of known algorithms). The third level of the problem complexity is the formation of skills and abilities of solving problems when the algorithm is unknown (research or heuristic). If the student has mastered a lower level of complexity, he can move on to the next. Such differentiated education is the most transparent and objective for students.

The successful application of professionally oriented problems in training of future engineers must meet the following didactic requirements:

- providing an organic connection between the material studied in the program of the mathematical course and professional problems arising in the activities of an engineer;
- practical significance of the selected professionally oriented problem;
- continuity, consistency and systematic application of such problems in teaching mathematics.

In the methodological literature there is no common classification of professionally oriented problems. However, the analysis of studying this issue allows us to classify problems with professional content according to the nature of the knowledge used, didactic principles, the ways of setting the problem conditions, the level of complexity and the methods of solution. Professionally oriented problems can be considered to explain a phenomenon or process; the means of problems are divided into text, graphic, tabular.

There are two main ways to solve such problems: algorithmic and heuristic. By means of the algorithmic method of solution, the way of solving the problem is known in advance, i.e. there is a ready solution algorithm. On the contrary, the heuristic method of solution requires selection and search of many solutions and is based mainly on mathematical intuition, the experience of previously solved problems, and consideration of previous mistakes.

Let us consider one of the problems on the theme "Application of a certain integral to pressure calculation".

Problem. Gas under atmospheric pressure is in a cylindrical container with forcer, the height $H = 2m$ and the radius $r = 0.5m$. Find the work that needs to be spent on gas compression with forcer of 1.5m. The gas temperature remains constant.

Solution.

According to the Boyle-Mariotte law, under isothermal compression, the relationship between pressure and volume will be:

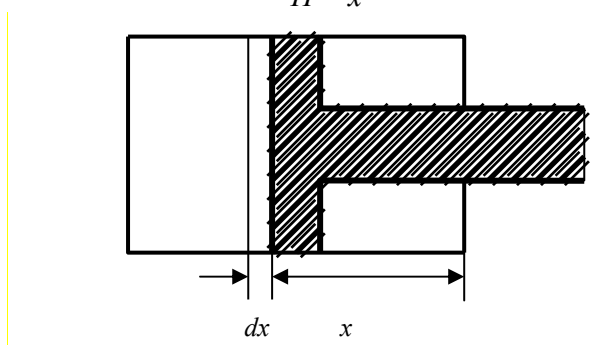
$$Pv = c. \quad c - const.$$

When the forcer moves at x m. (Fig. 4), the gas pressure per unit area is:

$$P(x) = \frac{c}{v(x)} = \frac{c}{S(H-x)},$$

where S - the area of forcer. Then

$$P(x) = \frac{c}{H-x} = SP(x)$$



Figure

Let the function $a(x)$ be the work to be spent on the movement of the forcer on x meters. Suppose that when the forcer moves on dx , the pressure on it $P(x)$ is constant. Find the approximate differential value of the function $a(x)$

$$\Delta a \approx P(x)dx = \frac{c}{H-x} dx = da$$

Next, we calculate the work when x changes from 0 to h :

$$A = c \int_0^h \frac{dx}{H-x} = -c \ln(H-x) \Big|_0^h = c \ln \frac{H}{H-h}$$

We calculate at $H=2m, h=1,5m, r=0,5m, P_0=10330kg/m^2$ (atmospheric pressure)

$$v_0 = \pi r^2 H = 0,5\pi$$

$$c = P_0 v_0 = 5165\pi.$$

We find the work to be spent on gas compression:

$$A \approx 5165\pi \cdot \ln \frac{2}{2-1,5} \approx 22494,4 \text{ \AA} \approx 220175,64 \quad (\text{\AA} \text{ \AA})$$

А.Ж. Сейтмұратов¹, З.А. Ергалауова², Л.С. Қайнабаева¹, Г.К. Ешмұрат¹

¹Қорқыт Ата атындағы Қызылорда мемлекеттік университеті. Қазақстан

²Абай атындағы қазақ ұлттық педагогикалық университеті. Қазақстан

ЖОО-НЫҢ ТЕХНИКАЛЫҚ МАМАНДЫҚТАРЫНДА МАТЕМАТИКАНЫ ОҚИТУДЫҢ КӘСІБИ БАҒЫТТЫЛЫҒЫНЫҢ ҚҰРАЛЫ РЕТІНДЕГІ МІНДЕТТЕР

Аннотация: Мақалада ЖОО-ның техникалық мамандықтарында математиканы оқытудың кәсіби бағыттылығы мәселесі қарастырылды, кәсіби мазмұнмен есептер мәселесі, оларды таңдау және саралау бойынша әдебиетке талдау жүргізілді. Болашақ инженерлерді табысты қолдану үшін оқытудағы кәсіби - бағытталған міндеттерге сәйкес келетін дидактикалық жағдайлар, кәсіби мазмұны бар есептерді жіктеу, сондай-ақ осындай міндеттерді шешу тәсілдері көрсетілген. Кәсіби мазмұны бар есептерге қойылатын негізгі талаптар көрсетілген, "қысымды есептеуге белгілі интегралды қолдану" тақырыбы бойынша есеп қарастырылды»

Түйінсөздер: міндеттері, күрделілік деңгейі, кәсіби бағыттылығы

А.Ж. Сейтмұратов¹, З.А. Ергалауова², Л.С. Қайнабаева¹, Г.К. Ешмұрат¹

¹Қызылординский государственный университет имени Коркыт Ата. Казахстан;

²Казахский национальный педагогический университет им. Абая. Казахстан

ЗАДАЧИ КАК СРЕДСТВО ПРОФЕССИОНАЛЬНОЙ НАПРАВЛЕННОСТИ ОБУЧЕНИЯ МАТЕМАТИКЕ НА ТЕХНИЧЕСКИХ СПЕЦИАЛЬНОСТЯХ ВУЗА

Аннотация: В статье рассмотрена проблема профессиональной направленности обучения математики на технических специальностях вуза, проведен анализ литературы по проблеме задач с профессиональным содержанием, их подбору и ранжированию. Показаны дидактические условия, которым должны соответствовать профессионально-ориентированные задачи в обучении будущих инженеров для их успешного применения, классификация задач с профессиональным содержанием, а также способы решения таких задач. Перечислены основные требования к задачам с профессиональным содержанием, рассмотрена задача по теме «Применение определенного интеграла к вычислению давления»

Ключевые слова: задача, уровень сложности, профессиональная направленность, классификация задач.

Information about the authors:

Seitmuratov Angisin – Doktor of Physical and Matematical Sciences, Professoz Korkyt Ata Kyzylorda State University, The Republic of Kazakstan. 120014 City of Kyzylorda, 29A Aitere bie str. angisin@mail.ru. <https://orcid.org/0000-0002-9622-9584>.

Yergalauova Zinegul – Doctoral student, Abai Kazakh National Pedagogical University, Kazakhstan. zina_73er@mail.ru. <https://orcid.org/0000-0002-9410-6425>.

Kainbayeva Larissa – Candidate of Pedagogical Sciences, Senior Lecturer, Korkyt Ata Kyzylorda state University, The Republic of Kazakstan. 120014 City of Kyzylorda, 29A Aitere bie str. larissa_kain@mail.ru. <https://orcid.org/0000-0002-2927-6575>.

Yeshmurat Gulnur – Master in Pedagogical Sciences, Lecturer, Korkyt Ata Kyzylorda State University, The Republic of Kazakstan. 120014 City of Kyzylorda, 29A Aitere bie str. gulnuresh@mail.ru. <https://orcid.org/0000-0002-3275-6457>.

REFERENCES

- [1] Vilenkin N.Ya., Mordkovich A.G. On the role of interdisciplinary relationship in the professional training of students of the pedagogical institute. // Problems of teacher training in pedagogical institutes. // Edited by N.Ya. Vilenkin, A.G. Mordkovich. M.: MSCPI, 1989. P.9-14.
- [2] Seitmuratov A., Taimuratova L., Zhussipbek B., Seitkhanova A., Kainbaeva L. Conditions of extreme stress state // News of the National Academy of Sciences of the Republic of Kazakhstan. Series of Geology and Technical Sciences. 2019. Volume 5, Number 437 (2019), 202 – 206 <https://doi.org/10.32014/2019.2518-170X.143>
- [3] Seitmuratov A., Tileubay S., Toksanova S., Ibragimova N., Doszhanov B., Aitimov M.Zh. The problem of the oscillation of the elastic layer bounded by rigid boundaries // News of NAS RK. Series of physico-mathematical. 2018(321): 42 – 48 (in Eng). ISSN 2518-1726 (Online), ISSN 1991-346X (Print). <https://doi.org/10.32014/2018.2518-1726.6>
- [4] Poya D. Mathematics and probable reasoning. M.: Nauka. 1985. P.463.
- [5] Seitmuratov A., Zharmenova B., Dauitbayeva A., Bekmuratova A. K., Tulegenova E., Ussenova G. Numerical analysis of the solution of some oscillation problems by the decomposition method // News of NAS RK. Series of physico-mathematical. 2019 1(323): 28 – 37 (in Eng). ISSN 2518-1726 (Online), ISSN 1991-346X (Print). <https://doi.org/10.32014/2019.2518-1726.4>
- [6] Seitmuratov A., Zhussipbek B., Sydykova G., Seithanova A., Aitimova U. Dynamic stability of wave processes of a round rod // News of NAS RK. Series of physico-mathematical. 2019 2(324): 90 – 98 (in Eng). ISSN 2518-1726 (Online), ISSN 1991-346X (Print). <https://doi.org/10.32014/2019.2518-1726.16>
- [7] Matyushkin A.M. Problem-solving situations in thinking and learning. M.: "Pedagogy", 1972. P.168.