

ISSN 2518-1726 (Online),  
ISSN 1991-346X (Print)

ҚАЗАҚСТАН РЕСПУБЛИКАСЫ  
ҰЛТТЫҚ ҒЫЛЫМ АКАДЕМИЯСЫНЫҢ  
Әль-фараби атындағы Қазақ ұлттық университетінің

# Х А Б А Р Л А Р Ы

---

---

## ИЗВЕСТИЯ

НАЦИОНАЛЬНОЙ АКАДЕМИИ НАУК  
РЕСПУБЛИКИ КАЗАХСТАН  
Қазақстан Республикасының  
Ғылым Академиясының  
Әль-Фараби атындағы  
Қазақ ұлттық университетінің

## NEWS

OF THE NATIONAL ACADEMY OF SCIENCES  
OF THE REPUBLIC OF KAZAKHSTAN  
Al-farabi kazakh  
national university

**SERIES  
PHYSICO-MATHEMATICAL**

**5 (327)**

**SEPTEMBER-OCTOBER 2019**

PUBLISHED SINCE JANUARY 1963

PUBLISHED 6 TIMES A YEAR

ALMATY, NAS RK

Б а с р е д а к т о р ы  
ф.-м.ғ.д., проф., ҚР ҰҒА академигі **Ғ.М. Мұтанов**

Р е д а к ц и я а л қ а с ы:

**Жұмаділдаев А.С.** проф., академик (Қазақстан)  
**Кальменов Т.Ш.** проф., академик (Қазақстан)  
**Жантаев Ж.Ш.** проф., корр.-мүшесі (Қазақстан)  
**Өмірбаев У.У.** проф. корр.-мүшесі (Қазақстан)  
**Жүсіпов М.А.** проф. (Қазақстан)  
**Жұмабаев Д.С.** проф. (Қазақстан)  
**Асанова А.Т.** проф. (Қазақстан)  
**Бошкаев К.А.** PhD докторы (Қазақстан)  
**Сұраған Д.** корр.-мүшесі (Қазақстан)  
**Quevedo Hernando** проф. (Мексика),  
**Джунушалиев В.Д.** проф. (Қырғыстан)  
**Вишневский И.Н.** проф., академик (Украина)  
**Ковалев А.М.** проф., академик (Украина)  
**Михалевич А.А.** проф., академик (Белорус)  
**Пашаев А.** проф., академик (Әзірбайжан)  
**Такибаев Н.Ж.** проф., академик (Қазақстан), бас ред. орынбасары  
**Тигиняну И.** проф., академик (Молдова)

**«ҚР ҰҒА Хабарлары. Физика-математикалық сериясы».**

**ISSN 2518-1726 (Online), ISSN 1991-346X (Print)**

Меншіктенуші: «Қазақстан Республикасының Ұлттық ғылым академиясы» РҚБ (Алматы қ.)  
Қазақстан республикасының Мәдениет пен ақпарат министрлігінің Ақпарат және мұрағат комитетінде  
01.06.2006 ж. берілген №5543-Ж мерзімдік басылым тіркеуіне қойылу туралы куәлік

Мерзімділігі: жылына 6 рет.  
Тиражы: 300 дана.

Редакцияның мекенжайы: 050010, Алматы қ., Шевченко көш., 28, 219 бөл., 220, тел.: 272-13-19, 272-13-18,  
<http://physics-mathematics.kz/index.php/en/archive>

---

© Қазақстан Республикасының Ұлттық ғылым академиясы, 2019

Типографияның мекенжайы: «Аруна» ЖК, Алматы қ., Муратбаева көш., 75.

Главный редактор  
д.ф.-м.н., проф. академик НАН РК **Г.М. Мутанов**

Редакционная коллегия:

**Джумадильдаев А.С.** проф., академик (Казахстан)  
**Кальменов Т.Ш.** проф., академик (Казахстан)  
**Жангаев Ж.Ш.** проф., чл.-корр. (Казахстан)  
**Умирбаев У.У.** проф., чл.-корр. (Казахстан)  
**Жусупов М.А.** проф. (Казахстан)  
**Джумабаев Д.С.** проф. (Казахстан)  
**Асанова А.Т.** проф. (Казахстан)  
**Бошкаев К.А.** доктор PhD (Казахстан)  
**Сураган Д.** чл.-корр. (Казахстан)  
**Quevedo Hernando** проф. (Мексика),  
**Джунушалиев В.Д.** проф. (Кыргызстан)  
**Вишневский И.Н.** проф., академик (Украина)  
**Ковалев А.М.** проф., академик (Украина)  
**Михалевич А.А.** проф., академик (Беларусь)  
**Пашаев А.** проф., академик (Азербайджан)  
**Такибаев Н.Ж.** проф., академик (Казахстан), зам. гл. ред.  
**Тигиняну И.** проф., академик (Молдова)

«Известия НАН РК. Серия физико-математическая».

ISSN 2518-1726 (Online), ISSN 1991-346X (Print)

Собственник: РОО «Национальная академия наук Республики Казахстан» (г. Алматы)

Свидетельство о постановке на учет периодического печатного издания в Комитете информации и архивов  
Министерства культуры и информации Республики Казахстан №5543-Ж, выданное 01.06.2006 г.

Периодичность: 6 раз в год.

Тираж: 300 экземпляров.

Адрес редакции: 050010, г. Алматы, ул. Шевченко, 28, ком. 219, 220, тел.: 272-13-19, 272-13-18,  
<http://physics-mathematics.kz/index.php/en/archive>

---

© Национальная академия наук Республики Казахстан, 2019

Адрес типографии: ИП «Аруна», г. Алматы, ул. Муратбаева, 75.

E d i t o r i n c h i e f  
doctor of physics and mathematics, professor, academician of NAS RK **G.M. Mutanov**

E d i t o r i a l b o a r d:

**Dzhumadildayev A.S.** prof., academician (Kazakhstan)  
**Kalmenov T.Sh.** prof., academician (Kazakhstan)  
**Zhantayev Zh.Sh.** prof., corr. member. (Kazakhstan)  
**Umirbayev U.U.** prof. corr. member. (Kazakhstan)  
**Zhusupov M.A.** prof. (Kazakhstan)  
**Dzhumabayev D.S.** prof. (Kazakhstan)  
**Asanova A.T.** prof. (Kazakhstan)  
**Boshkayev K.A.** PhD (Kazakhstan)  
**Suragan D.** corr. member. (Kazakhstan)  
**Quevedo Hernando** prof. (Mexico),  
**Dzhunushaliyev V.D.** prof. (Kyrgyzstan)  
**Vishnevskiy I.N.** prof., academician (Ukraine)  
**Kovalev A.M.** prof., academician (Ukraine)  
**Mikhalevich A.A.** prof., academician (Belarus)  
**Pashayev A.** prof., academician (Azerbaijan)  
**Takibayev N.Zh.** prof., academician (Kazakhstan), deputy editor in chief.  
**Tiginyanu I.** prof., academician (Moldova)

**News of the National Academy of Sciences of the Republic of Kazakhstan. Physical-mathematical series.**

**ISSN 2518-1726 (Online), ISSN 1991-346X (Print)**

Owner: RPA "National Academy of Sciences of the Republic of Kazakhstan" (Almaty)

The certificate of registration of a periodic printed publication in the Committee of information and archives of the Ministry of culture and information of the Republic of Kazakhstan N 5543-Ж, issued 01.06.2006

Periodicity: 6 times a year

Circulation: 300 copies

Editorial address: 28, Shevchenko str., of. 219, 220, Almaty, 050010, tel. 272-13-19, 272-13-18,  
<http://physics-mathematics.kz/index.php/en/archive>

---

© National Academy of Sciences of the Republic of Kazakhstan, 2019

Address of printing house: ST "Aruna", 75, Muratbayev str, Almaty

## NEWS

OF THE NATIONAL ACADEMY OF SCIENCES OF THE REPUBLIC OF KAZAKHSTAN  
 PHYSICO-MATHEMATICAL SERIES

ISSN 1991-346X

<https://doi.org/10.32014/2019.2518-1726.58>

Volume 5, Number 327 (2019), 51 – 58

**K.B. Jakupov**

Institute of mathematics and mathematical modeling, Almaty, Kazakhstan.  
 Kazak National University named after Al-Farabi  
[jakupovKB@mail.ru](mailto:jakupovKB@mail.ru)

## FALSIFICATIONS OF THE ENERGY BALANCE EQUATION, PUASSON ADIABATS AND LAPLACE SOUND SPEED

**Abstract.** The falsity of the energy balance equation with a specific heat capacity coefficient at constant pressure, the fake Poisson adiabat, and the fake Laplace formula of adiabatic sound velocity are established. Universal formulas of adiabatic ideal gas and sound velocity are proposed and substantiated. Bibl.10.

**Keywords:** equation, sound, heat capacity, adiabat, isobaric.

1. Falsifications of the heat equation with specific coefficient of heat capacity at constant pressure

Scalar product of the equation of dynamics

$$\rho \frac{d\mathbf{v}}{dt} = \rho \mathbf{F} + \frac{\partial \mathbf{p}_x}{\partial x} + \frac{\partial \mathbf{p}_y}{\partial y} + \frac{\partial \mathbf{p}_z}{\partial z} + \mathbf{f}$$

on speed gives kinetic energy equation

$$\rho \frac{d\mathbf{v}}{dt} \cdot \mathbf{v} = \rho \mathbf{F} \cdot \mathbf{v} + \frac{\partial \mathbf{p}_x}{\partial x} \cdot \mathbf{v} + \frac{\partial \mathbf{p}_y}{\partial y} \cdot \mathbf{v} + \frac{\partial \mathbf{p}_z}{\partial z} \cdot \mathbf{v} + \mathbf{f} \cdot \mathbf{v}, \quad (1.1)$$

which is part of the energy balance equation

$$\rho \frac{d}{dt} (E + |\mathbf{v}|^2 / 2) = \rho \mathbf{F} \cdot \mathbf{v} + \mathbf{f} \cdot \mathbf{v} + \frac{\partial}{\partial x} \mathbf{p}_x \cdot \mathbf{v} + \frac{\partial}{\partial y} \mathbf{p}_y \cdot \mathbf{v} + \frac{\partial}{\partial z} \mathbf{p}_z \cdot \mathbf{v} - \nabla \cdot \mathbf{q} + \rho Q,$$

as can be seen from the following:

$$\begin{aligned} \rho \frac{dE}{dt} + \rho \frac{d\mathbf{v}}{dt} \cdot \mathbf{v} &= \rho \mathbf{F} \cdot \mathbf{v} + \mathbf{f} \cdot \mathbf{v} + \frac{\partial \mathbf{p}_x}{\partial x} \cdot \mathbf{v} + \mathbf{p}_x \cdot \frac{\partial \mathbf{v}}{\partial x} + \frac{\partial \mathbf{p}_y}{\partial x} \cdot \mathbf{v} + \mathbf{p}_y \cdot \frac{\partial \mathbf{v}}{\partial y} + \\ &+ \frac{\partial \mathbf{p}_z}{\partial z} \cdot \mathbf{v} + \mathbf{p}_z \cdot \frac{\partial \mathbf{v}}{\partial z} - \nabla \cdot \mathbf{q} + \rho Q \end{aligned}$$

The abbreviation for (1.1) leads to the equation

$$\rho \frac{dE}{dt} = \mathbf{p}_x \cdot \frac{\partial \mathbf{v}}{\partial x} + \mathbf{p}_y \cdot \frac{\partial \mathbf{v}}{\partial y} + \mathbf{p}_z \cdot \frac{\partial \mathbf{v}}{\partial z} - \nabla \cdot \mathbf{q} + \rho Q$$

from which for the internal energy  $dE = c_v dT$  and according to the Fourier law  $\mathbf{q} = -\lambda \nabla T$  we obtain various representations of the heat equation, respectively, to the stress tensors.

With asymmetric stress tensor for Newton's law of friction:

$$\rho c_v \frac{dT}{dt} = \nabla \cdot (\lambda \nabla T) - p \nabla \cdot \mathbf{v} + \mu \sum_{i=1}^3 \sum_{j=1}^3 \left( \frac{\partial v_i}{\partial x_j} \right)^2 + \rho Q$$

with an asymmetric tensor of the Jakupov [9-10] friction law:

$$\rho c_v \frac{dT}{dt} = \nabla \cdot (\lambda \nabla T) - p \nabla \cdot \mathbf{v} + \sum_{j=1}^3 \sum_{i=1}^3 \frac{\alpha \mu}{m_i^{m_i-1}} \frac{\partial v_i^{m_i}}{\partial x_j} \frac{\partial v_i}{\partial x_j} + \rho Q, \quad \alpha = 1 \left( \frac{cek}{M} \right)^{m_i-1}$$

and the heat equation with the symmetric Stokes stress tensor [1-8]:

$$\rho c_v \frac{dT}{dt} = \nabla \cdot (\lambda \nabla T) - p \nabla \cdot \mathbf{v} + \frac{\mu}{2} \sum_{i=1}^3 \sum_{j=1}^3 \left( \frac{\partial v_i}{\partial x_j} + \frac{\partial v_j}{\partial x_i} \right)^2 - \frac{2}{3} \mu (\nabla \cdot \mathbf{v})^2, \quad (1.2)$$

which is false due to the falseness of the Stokes stress tensor [9-10].

Let us pay attention to the fact that these equations include the coefficient  $C_v$  of the specific heat capacity of a gas with a constant volume, according to the 1st law of thermodynamics.

In addition to the fact that the heat conduction equation is fake according to the Stokes friction law, the tendency to transform into an equation with the specific heat coefficient of gas  $C_p$  at constant pressure [1-9] is well known.

Specifically, Lykov (see [3] p. 32) gives the following equation:

$$\rho c_p \frac{dT}{dt} - \frac{dp}{dt} = \lambda \nabla^2 T + \frac{\mu}{2} \sum_{i=1}^3 \sum_{j=1}^3 \left( \frac{\partial v_i}{\partial x_j} + \frac{\partial v_j}{\partial x_i} \right)^2 - \frac{2}{3} \mu (\nabla \cdot \mathbf{v})^2 \quad (1.3)$$

For the derivation, the universal gas constant and the Clapeyron-Mendeleev state equation are used

$$c_p - c_v = R, \quad p = \rho RT \quad (1.4)$$

Using (1.4) in the error equation (1.2), substitutions are made

$$\begin{aligned} c_v T &= (c_p - R)T = c_p T - RT = c_p T - \frac{p}{\rho}, \\ \rho c_v \frac{dT}{dt} &= \rho \left( c_p \frac{dT}{dt} - \frac{d}{dt} \frac{p}{\rho} \right) = \rho \left[ c_p \frac{dT}{dt} - \frac{1}{\rho^2} \left( \rho \frac{dp}{dt} - p \frac{d\rho}{dt} \right) \right] = \\ &= \rho c_p \frac{dT}{dt} - \frac{dp}{dt} + \frac{p}{\rho} \frac{d\rho}{dt} \end{aligned}$$

where by the continuity equation  $\frac{1}{\rho} \frac{d\rho}{dt} = -\nabla \cdot \mathbf{v}$ . Therefore

$$\rho c_v \frac{dT}{dt} = \rho c_p \frac{dT}{dt} - \frac{dp}{dt} + \frac{p}{\rho} \frac{d\rho}{dt} = \rho c_p \frac{dT}{dt} - \frac{dp}{dt} - p \nabla \cdot \mathbf{v}$$

Substitution in the equation (1.2) gives

$$\rho c_p \frac{dT}{dt} - \frac{dp}{dt} - p \nabla \cdot \mathbf{v} = \nabla \cdot (\lambda \nabla T) - p \nabla \cdot \mathbf{v} + \frac{\mu}{2} \sum_{i=1}^3 \sum_{j=1}^3 \left( \frac{\partial v_i}{\partial x_j} + \frac{\partial v_j}{\partial x_i} \right)^2 - \frac{2}{3} \mu (\nabla \cdot \mathbf{v})^2$$

After contractions and rearrangements, the equation is obtained

$$\rho c_p \frac{dT}{dt} = \nabla \cdot (\lambda \nabla T) + \frac{dp}{dt} + \frac{\mu}{2} \sum_{i=1}^3 \sum_{j=1}^3 \left( \frac{\partial v_i}{\partial x_j} + \frac{\partial v_j}{\partial x_i} \right)^2 - \frac{2}{3} \mu (\nabla \cdot \mathbf{v})^2 \quad (1.5)$$

For constant thermal conductivity coefficient  $\lambda = \text{const}$  equation (1.5) goes over to the Lykov equation (1.3).

**Theorem.** The equation of heat conduction with the coefficient of specific heat capacity of gas at constant pressure

$$\rho c_p \frac{dT}{dt} = \nabla \cdot (\lambda \nabla T) + \frac{dp}{dt} + \frac{\mu}{2} \sum_{i=1}^3 \sum_{j=1}^3 \left( \frac{\partial v_i}{\partial x_j} + \frac{\partial v_j}{\partial x_i} \right)^2 - \frac{2}{3} \mu (\nabla \cdot \mathbf{v})^2$$

is fake in flows with variable pressure, as formula  $C_p - C_v =$  is valid only for constant pressure  $p = \text{const}$ .

*Evidence.* The 1st law of thermodynamics is attracted [7]:

$$d'Q = dE + pdV \quad (1.6)$$

In an ideal gas  $dE = c_v dT$ ,  $c_v$  is the coefficient of specific heat of gas at a constant volume. Between the specific volume  $V$  and the density of the gas there is a connection  $V = \frac{1}{\rho}$ ,  $dV = d\left(\frac{1}{\rho}\right)$ .

Therefore, the 1st law is used in the form [1]:

$$d'Q = c_v dT + pd\left(\frac{1}{\rho}\right), \quad d'Q = c_v dT + pd\left(\frac{RT}{p}\right) \quad (1.7)$$

Let the heat be supplied to the gas at a constant volume of  $V = \text{const}$ . Since  $dV = 0$  in this case it follows from (1.6)  $d'Q = dE = c_v dT$ .

Let heat be supplied to gas  $d'Q = c_p dT$  with constant pressure  $p = \text{const}$ .

The 1st law of thermodynamics (1.7) is converted to the form

$$c_p dT = c_v dT + pd\left(\frac{RT}{p}\right), \quad (c_p - c_v)dT = p \frac{pd(RT) - RTdp}{p^2},$$

$$(c_p - c_v)dT = RdT - RT \frac{dp}{p}, \quad p = \rho RT$$

Dividing the last equality by  $dT$  we obtain the following formula for a universal gas constant:

$$R = c_p - c_v + \frac{1}{\rho} \frac{dp}{dT}, \quad (1.8)$$

At constant pressure  $p = \text{const}$ ,  $dp = 0$  from (1.8) we get the formula widely used in gas dynamics [1-9]:

$$R = c_p - c_v \quad (1.9)$$

By virtue of (1.8) in non-isobaric gas flows with variable pressure  $p \neq \text{const}$ ,  $dp \neq 0$ , there will always be inequality  $R \neq c_p - c_v$ !

This axiom is also evident from the 1st law of thermodynamics

$$d'Q = c_v dT + pd\left(\frac{RT}{p}\right), \quad d'Q = c_v dT + p \frac{pd(RT) - RTdp}{p^2},$$

$$d'Q = c_v dT + R dT - RT \frac{dp}{p}, \quad d'Q = c_v dT + R dT - \frac{1}{\rho} dp$$

For universal constant gas, dividing the last expression on the temperature differential, we get the formula

$$R = \frac{d'Q}{dT} - c_v + \frac{1}{\rho} \frac{dp}{dT} \quad (1.10)$$

It is obvious, by virtue of equality (1.10), that in non-isobaric flows of gas with variable pressure  $p \neq \text{const}$ ,  $dp \neq 0$ , inequality

$$R \neq c_p - c_v!$$

Consequently, the heat conduction equation with a coefficient  $C_p$  of the specific heat of a gas at constant pressure is false, since it is obtained for connection  $C_p - C_v = R$ , which does not hold for variable pressure  $p \neq \text{const}$ .

What was required to prove.

## 2. Falsifications of Poisson adiabat

In the dynamics of an ideal gas, a false heat equation (1.5) for enthalpy  $h = c_p T$ ,  $\lambda \equiv 0$ ,  $\mu \equiv 0$  takes the form (see [1] p. 115):

$$\rho c_p \frac{dT}{dt} = \frac{dp}{dt}, \quad \rho \frac{dh}{dt} = \frac{dp}{dt}, \quad (2.1)$$

therefore, it is also false.

Reducing the differential in time gives the connection

$$dp = \rho c_p dT \quad (2.2)$$

From the fake equation (2.2), converted to Form  $\frac{dp}{\rho} = c_p dT$ , again using  $R = c_p - c_v$ , which is valid only for constant pressure, the Poisson adiabat is displayed (see Loitsyansky [1] p.115):

$$\frac{dp}{\rho} = c_p dT = \frac{c_p}{R} d(RT) = \frac{c_p}{c_p - c_v} d\left(\frac{p}{\rho}\right), \quad \frac{dp}{\rho} = k \frac{d\rho}{\rho}, \quad \frac{p}{p_0} = \left(\frac{\rho}{\rho_0}\right)^k, \quad k = \frac{c_p}{c_v}$$

Calculate the pressure differential using the Clapeyron-Mendeleev equation of state  $p = R\rho T$  :

$$dp = \rho R dT + TR d\rho$$

Similarly, assuming in this ratio  $R = c_p - c_v$ , just used to derive the Poisson adiabat, we get the true value of the pressure differential

$$dp = \rho(c_p - c_v) dT + TR d\rho,$$

whose transformed expression

$$dp = \rho c_p dT - \rho c_v dT + TR d\rho, \quad \frac{dp}{dt} = \rho \frac{dh}{dt} - \rho c_v \frac{dT}{dt} + TR \frac{d\rho}{dt} \quad (2.3)$$

does not coincide with the differential (2.2) and equation (2.1) !!!

The difference between (2.2) and (2.3) is not equal to zero:

$$- \rho c_v dT + TR d\rho \neq 0$$



Consequently, the differential pressure  $dp = \rho c_p dT$  (2.2), corresponding to a fake heat equation with a heat capacity coefficient at constant pressure is also fake.

The falsity of equations (2.1) is proven again.

Proved inequality  $\rho \frac{dh}{dt} \neq \frac{dp}{dt}!$

From fake equality  $\rho \frac{dh}{dt} = \frac{dp}{dt}$ , the Poisson adiabat [1] is derived, consequently, the Poisson adiabat is also fake !!!

As is known, the Poisson adiabat is widely used in gas dynamics, for example, when calculating the propagation velocity of small perturbations, i.e. speed of sound.

### 3. Falsification of the speed of sound of Laplace

On the basis of the equation of Clapeyron –Mendeleeva Newton derived the isothermal speed of sound

$$a = \sqrt{\frac{\partial p}{\partial \rho}} = \sqrt{\frac{\partial(\rho RT)}{\partial \rho}} = \sqrt{RT}, \quad a = \sqrt{\frac{p}{\rho}}$$

Laplace proposed to use the Poisson adiabat  $p = p_0 \left(\frac{\rho}{\rho_0}\right)^k$ :

$$a = \sqrt{\frac{\partial p}{\partial \rho}} = \sqrt{\frac{\partial}{\partial \rho} \left(p_0 \left(\frac{\rho}{\rho_0}\right)^k\right)} = \sqrt{k \frac{p}{\rho}}, \quad a = \sqrt{kRT} \quad (3.1)$$

Connection  $R = c_p - c_v$  takes place only for constant pressure  $p = const$ , therefore, the Laplace formula (3.1) is not only adiabatic, but also isobaric sound speed.

Consequently, due to the falsity of the Poisson adiabat, it is logical to consider the formula (3.1) to be the adiabatic and isobaric Laplace sound velocity as fake.

Using a fake link  $\rho c_p dT = dp$  and the equation of state Clapeyron-Mendeleev, we organize the calculations:

$$\frac{dp}{\rho} = c_p dT = \frac{c_p}{R} d(RT) = \frac{c_p}{R} d\left(\frac{p}{\rho}\right), \quad \frac{c_p}{R} d\left(\frac{p}{\rho}\right) = \frac{dp}{\rho}, \quad \frac{c_p}{R} \cdot \frac{\rho dp - p d\rho}{\rho^2} = \frac{dp}{\rho},$$

$$\frac{c_p}{R} dp - \frac{c_p}{R} \cdot p \frac{d\rho}{\rho} = dp, \quad \left(\frac{c_p}{R} - 1\right) dp = \frac{c_p}{R} \cdot p \frac{d\rho}{\rho}, \quad \left(\frac{c_p}{R} - 1\right) \frac{dp}{p} = \frac{c_p}{R} \frac{d\rho}{\rho},$$

$$\frac{c_p - R}{R} d \ln p = \frac{c_p}{R} d \ln \rho, \quad d \ln p - \frac{c_p}{c_p - R} d \ln \rho = 0,$$

$$\ln \frac{p}{\rho^\chi} = const, \quad \frac{p}{p_0} = \left(\frac{\rho}{\rho_0}\right)^\chi, \quad \chi = \frac{c_p}{c_p - R}$$

So, from the false connection  $\rho c_p dT = dp$  we get the adiabat

$$\frac{p}{p_0} = \left(\frac{\rho}{\rho_0}\right)^\chi, \quad \chi = \frac{c_p}{c_p - R}, \quad (3.2)$$

which for  $R = c_p - c_v$  goes to the Poisson adiabat.

Calculate the speed of sound:

$$a = \sqrt{\frac{\partial p}{\partial \rho}} = \sqrt{\frac{\partial}{\partial \rho} (p_0 (\frac{\rho}{\rho_0})^\chi)} = \sqrt{\frac{p_0}{\rho_0^\chi} \chi \rho^{\chi-1}} =$$

$$= \sqrt{\frac{p_0}{\rho} \chi (\frac{\rho}{\rho_0})^\chi} = \sqrt{\frac{c_p}{c_p - R} \frac{p}{\rho}}$$

So, for the speed of sound, the formula is obtained (also fake, as in Laplace)

$$a = \sqrt{\frac{c_p}{c_p - R} \frac{p}{\rho}}, \quad a = \sqrt{\frac{c_p}{c_p - R} RT},$$

which for  $R = c_p - c_v$  goes to the Laplace formula (3.1).

#### 4. Universal adiabatic sound speed

The 1st law of thermodynamics  $d'Q = dE + pd(\frac{1}{\rho})$  in an adiabatic gas (heat is not removed and not supplied  $d'Q = 0$ ):

$$0 = dE + pd(\frac{1}{\rho}), \quad dE = c_v dT \quad (4.1)$$

According to the equation of state of Clapeyron-Mendeleev we find:

$$0 = c_v dT + pd(\frac{1}{\rho}), \quad 0 = c_v d(\frac{p}{R\rho}) - p \frac{d\rho}{\rho^2}$$

Next are the necessary conversions:

$$0 = \frac{c_v}{R} \cdot \frac{\rho dp - p d\rho}{\rho^2} - p \frac{d\rho}{\rho^2}, \quad 0 = \frac{c_v}{R} \cdot (\rho dp - p d\rho) - p d\rho,$$

$$0 = \frac{c_v}{R} \cdot (\frac{dp}{p} - \frac{d\rho}{\rho}) - \frac{d\rho}{\rho}, \quad \frac{c_v}{R} \cdot \frac{dp}{p} = (\frac{c_v}{R} + 1) \frac{d\rho}{\rho}, \quad \frac{dp}{p} = (\frac{R}{c_v} + 1) \frac{d\rho}{\rho}$$

From the last equality follows adiabat (Jakupov)\*:

$$\frac{p}{p_0} = (\frac{\rho}{\rho_0})^\zeta, \quad \zeta = \frac{R}{c_v} + 1$$

which for  $R = c_p - c_v$ , i.e. for constant pressure too goes to the Poisson adiabat.

So, the logic for the speed of sound is the formula (Jakupov)\*

$$a = \sqrt{\frac{\partial p}{\partial \rho}} = \sqrt{\left(\frac{R}{c_v} + 1\right) \frac{p}{\rho}}, \quad a = \sqrt{\left(\frac{R}{c_v} + 1\right) RT},$$

which, for a constant pressure, when performing  $R = c_p - c_v$ , goes to the

### Laplace formula (3.1).

Note. The barometric formula [7]  $p = p_0 \exp\left(-\frac{Mgz}{RT}\right)$  confirms the fact that even in a stationary atmosphere  $V = 0$  pressure is a variable function.

\* These adiabatic names and the universal formula for the speed of sound are necessary to emphasize novelty and differences from the Poisson and Laplace formulas.

### К. Б. Жақып-тегі

ҚР БҒМ Математика және математикалық моделдеу институты, Алматы, Қазақстан  
Аль-Фараби атындағы Қазақ Ұлттық Университеті, Алматы, Қазақстан

### ПУАССОННЫҢ АДИАБАТАСЫНЫҢ, ЛАПЛАСТЫҢ ДЫБЫС ЖЫЛДАМДЫҒЫНЫҢ ЖӘНЕ ЭНЕРГИЯЛАР БАЛАНСЫНЫҢ ТЕНДЕУІНІҢ ЖАЛҒАНДЫҚТАРЫ

**Аннотация.** Қысым тұрақтылықтығы, жылусыйымдылық еселеуіші бар энергиялар балансының жалғандығы, сонымен қатар Пуассонның адиабатасының және Лапластың дыбыс жылдамдығының кейітемелерінің қателіктері нақты дәлелделінген. Идеалдық газдардың адиабатасының кейіптемесі орнатылған, оған байланысты дыбыс жылдамдығының жаңадан универсалдық тұрпаты негізделген. Библ.10.

**Түйін сөздер:** тендеу, жылусыйымдылық, адиабата, изобарлық.

УДК 532.533

### К.Б. Джакупов

Институт математики и математического моделирования МОН РК, Алматы, Казахстан  
Казахский Национальный Университет им.Аль-Фараби, Алматы, Казахстан

### ФАЛЬСИФИКАЦИИ УРАВНЕНИЯ БАЛАНСА ЭНЕРГИЙ, АДИАБАТЫ ПУАССОНА И СКОРОСТИ ЗВУКА ЛАПЛАСА

**Аннотация.** Установлены фальшивость уравнения баланса энергий с удельным коэффициентом теплоемкости при постоянном давлении, фальшивость адиабаты Пуассона и фальшивость формулы Лапласа адиабатической скорости звука. Предложены и обоснованы универсальные формулы адиабаты идеального газа и скорости звука. Библ.10.

**Ключевые слова:** уравнение, звук, теплоемкость, адиабата, изобарический.

#### Information about the author:

Jakupov Kenes Bazhkenovitch - Doctor of Physical and Mathematical Sciences Professor, Academician of the Russian Academy of Natural Sciences. Service Address: RSE Institute of Mathematics and Mathematical modeling of the CM MES RK, 050010, Pushkin St., 125, Almaty, Kazakhstan, **Telephone:** 8 727 305 92 44, +7 701 667 88 59, [jakupovKB@mail.ru](mailto:jakupovKB@mail.ru), <https://orcid.org/0000-0003-1097-2893>

**REFERENCES**

- [1] Loitsyansky L.G. Fluid and gas mechanics. M.: "Science", 1973.
- [2] Sedov L.I. Continuum mechanics. T.1. M.: "Science", 1973.
- [3] Lykov A.V. Thermal Mass Transfer. M.: "Energy", 1972. P.560.
- [4] George E. Mase. Theory and Problems of Continuum Mechanics. Schaum's Outline Series. MCGRAW-HILL BOOK COMPANY. NewYork, St. Louis, San Francisco, London 1970.
- [5] Batchelor J. Introduction to fluid dynamics. M.: Mir, 1973
- [6] Landau L. D., Lifshchits E.M. Hydrodynamics. M.: "Science", 1973.
- [7] Saveliev IV. The course of general physics. Vol. 1. M.: "Science", 1977.
- [8] Schlichting G. Theory of the boundary layer. M.: "Science", 1974.
- [9] Jakupov K.B. RHEOLOGICAL LAWS OF VISCOUS FLUID DYNAMICS // NEWS of the National Academy of Sciences of the Republic of Kazakhstan, physico-mathematical Series, 1(293), 2014r.c.51-55. I SSN 1991-346X.
- [10] Jakupov K.B. Elimination of falsifications and modernization of the foundations of mechanics Continuous environment - Almaty: Publishing house "The White Orders", 2017. C.435. ISBN 978-601-280-859-9
- [11] Jakupov K.B. NATURAL FILTRATION EQUATIONS. FIASCO "OF DARCY'S LAW" //NEWS of the National Academy of Sciences of the Republic of Kazakhstan, physico-mathematical Series, 6(322), 2018, p.54-70. ISSN 2518-1726(Online), ISSN 1991 346X (Print), DOI <https://doi.org/10.32014/2018.2518-1726.18>
- [12] Jakupov K.B. NONLINEAR LAW OF HONEY IN THE THEORY OF ELASTICITY OF INHOMOGENEOUS AND ANISOTROPIC BODIES//NEWS of the National Academy of Sciences of the Republic of Kazakhstan, physico-mathematical Series, 1(317), 2018, p.63-74. ISSN 1991 346X (Print), ISSN 2518-1726(Online)

## **Publication Ethics and Publication Malpractice in the journals of the National Academy of Sciences of the Republic of Kazakhstan**

For information on Ethics in publishing and Ethical guidelines for journal publication see <http://www.elsevier.com/publishingethics> and <http://www.elsevier.com/journal-authors/ethics>.

Submission of an article to the National Academy of Sciences of the Republic of Kazakhstan implies that the described work has not been published previously (except in the form of an abstract or as part of a published lecture or academic thesis or as an electronic preprint, see <http://www.elsevier.com/postingpolicy>), that it is not under consideration for publication elsewhere, that its publication is approved by all authors and tacitly or explicitly by the responsible authorities where the work was carried out, and that, if accepted, it will not be published elsewhere in the same form, in English or in any other language, including electronically without the written consent of the copyright-holder. In particular, translations into English of papers already published in another language are not accepted.

No other forms of scientific misconduct are allowed, such as plagiarism, falsification, fraudulent data, incorrect interpretation of other works, incorrect citations, etc. The National Academy of Sciences of the Republic of Kazakhstan follows the Code of Conduct of the Committee on Publication Ethics (COPE), and follows the COPE Flowcharts for Resolving Cases of Suspected Misconduct ([http://publicationethics.org/files/u2/New\\_Code.pdf](http://publicationethics.org/files/u2/New_Code.pdf)). To verify originality, your article may be checked by the Cross Check originality detection service <http://www.elsevier.com/editors/plagdetect>.

The authors are obliged to participate in peer review process and be ready to provide corrections, clarifications, retractions and apologies when needed. All authors of a paper should have significantly contributed to the research.

The reviewers should provide objective judgments and should point out relevant published works which are not yet cited. Reviewed articles should be treated confidentially. The reviewers will be chosen in such a way that there is no conflict of interests with respect to the research, the authors and/or the research funders.

The editors have complete responsibility and authority to reject or accept a paper, and they will only accept a paper when reasonably certain. They will preserve anonymity of reviewers and promote publication of corrections, clarifications, retractions and apologies when needed. The acceptance of a paper automatically implies the copyright transfer to the National Academy of Sciences of the Republic of Kazakhstan.

The Editorial Board of the National Academy of Sciences of the Republic of Kazakhstan will monitor and safeguard publishing ethics.

Правила оформления статьи для публикации в журнале смотреть на сайтах:

[www:nauka-nanrk.kz](http://www.nauka-nanrk.kz)

<http://physics-mathematics.kz/index.php/en/archive>

**ISSN 2518-1726 (Online), ISSN 1991-346X (Print)**

Редакторы *М. С. Ахметова, Т.А. Апендиев, Д.С. Аленов*  
Верстка на компьютере *А.М. Кульгинбаевой*

Подписано в печать 10.10.2019.  
Формат 60x881/8. Бумага офсетная. Печать – ризограф.  
9,6 п.л. Тираж 300. Заказ 5.